

A minimum problem

Find the shortest distance from the origin O to the curve $y = \frac{1}{x^4}$ (where $x > 0$).

Use the following methods:

(1) Calculus,

(2) A.M. \geq G.M.

